

Quiz:

1. Compute the antiderivatives of the following.

(2) a. $f(x) = \sin x$
 $F(x) = -\cos(x)$

(2) b. $g(x) = x^2 + 3x + \sec^2(x)$
 $G(x) = \frac{1}{3}x^3 + \frac{3}{2}x^2 + \tan(x)$

(2) c. $h(x) = 1 + x - 3x^2$
 $H(x) = x + \frac{1}{2}x^2 - x^3$

(4) 2. Compute the area under $y = x^2 + 1$ from $x = 0$ to $x = 1$.

$$A = \lim_{n \rightarrow \infty} \sum_{i=1}^n f(x_i) \Delta x$$

$$\Delta x = \frac{1-0}{n} = \frac{1}{n}$$

$$x_i = 0 + \Delta x i = \frac{i}{n}$$

$$= \lim_{n \rightarrow \infty} \sum_{i=1}^n \left(\frac{i^2}{n^2} + 1 \right) \frac{1}{n} = \lim_{n \rightarrow \infty} \left[\frac{1}{n^3} \sum_{i=1}^n i^2 + \frac{1}{n} \sum_{i=1}^n 1 \right]$$

$$= \lim_{n \rightarrow \infty} \left[\frac{n(n+1)(2n+1)}{6n^3} + \frac{1}{n} (n) \right]$$

$$= \lim_{n \rightarrow \infty} \left[\frac{2n^3 + 3n^2 + n}{6n^3} + 1 \right] = \lim_{n \rightarrow \infty} \left[\frac{2 + \frac{3}{n} + \frac{1}{n^2}}{6} + 1 \right]$$

$$= \frac{1}{3} + 1 = \frac{4}{3}$$