MthSc 208: Differential Equations (Fall 2011) In-class Worksheet 1a: Plotting slope fields

NAME:

Consider the ODE y' = 2y + t.

(a) Draw the ty-plane (i.e., t on the x-axis, and y(t) on the x-axis). Draw a dot at each integer lattice point at each (t, y), where t, y = -1, 0, 1.

(b) At each of these nine points, compute y'(t). On the ty-plane, draw a "hash mark" at (t, y) with slope y'(t).

Written by M. Macauley

- (c) Now, we will use a better method to sketch the slope field. Determine the set of points for which y' = 0 (it will be a line set y' = 0 and solve for y.)
- (d) Repeat the previous step except for y'=c, for various values of c: 1, 2, 3, -1, $-\frac{1}{2}$.

(e) Sketch the lines you found above on the ty-plane. Along each line, sketch the hash-marks of the corresponding slope, y'=c.

(f) In the slope field above, sketch the three particular solution curves that satisfy y(0) = 1, $y(0) = -\frac{3}{4}$, and $y(1) = -\frac{3}{4}$, respectively.

Written by M. Macauley 2