## MthSc 208: Differential Equations (Fall 2011) <br> In-class Worksheet 1a: Plotting slope fields

NAME:

Consider the ODE $y^{\prime}=2 y+t$.
(a) Draw the $t y$-plane (i.e., $t$ on the $x$-axis, and $y(t)$ on the $x$-axis). Draw a dot at each integer lattice point at each $(t, y)$, where $t, y=-1,0,1$.
(b) At each of these nine points, compute $y^{\prime}(t)$. On the $t y$-plane, draw a "hash mark" at $(t, y)$ with slope $y^{\prime}(t)$.
(c) Now, we will use a better method to sketch the slope field. Determine the set of points for which $y^{\prime}=0$ (it will be a line - set $y^{\prime}=0$ and solve for $y$.)
(d) Repeat the previous step except for $y^{\prime}=c$, for various values of $c: 1,2,3,-1,-\frac{1}{2}$.
(e) Sketch the lines you found above on the ty-plane. Along each line, sketch the hash-marks of the corresponding slope, $y^{\prime}=c$.
(f) In the slope field above, sketch the three particular solution curves that satisfy $y(0)=1, y(0)=-\frac{3}{4}$, and $y(1)=-\frac{3}{4}$, respectively.

