MthSc 208 (Fall 2011) Worksheet 5f

MthSc 208: Differential Equations (Fall 2011) In-class Worksheet 5f: ODEs with Piecewise Forcing Terms

NAME:

Consider the initial value problem y'' + y = f(t), y(0) = 0, y'(0) = 1, where $f(t) = \begin{cases} 2t, & 0 \le t \le 1 \\ 2, & t > 1 \end{cases}$

1. Sketch f(t), and write it using the Heavyside function.

2. Take the Laplace transform of the differential equation, and solve for Y(s).

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3. Use partial fractions to decompose Y(s) into four terms. [Note: $\frac{1}{s^2(s^2+1)} = \frac{1}{s^2} - \frac{1}{s^2+1}$.]

4. Apply the inverse Laplace transfrom to each term and write the solution to the IVP using the Heavyside function.

5. Write the solution as a piecewise function (i.e., *not* using the Heavyside function).