## MthSc 208: Differential Equations (Fall 2011) In-class Worksheet 5f: ODEs with Piecewise Forcing Terms

## NAME:

Consider the initial value problem $y^{\prime \prime}+y=f(t), y(0)=0, y^{\prime}(0)=1$, where $f(t)= \begin{cases}2 t, & 0 \leq t \leq 1 \\ 2, & t>1\end{cases}$

1. Sketch $f(t)$, and write it using the Heavyside function.
2. Take the Laplace transform of the differential equation, and solve for $Y(s)$.
3. Use partial fractions to decompose $Y(s)$ into four terms. [Note: $\frac{1}{s^{2}\left(s^{2}+1\right)}=\frac{1}{s^{2}}-\frac{1}{s^{2}+1}$.]
4. Apply the inverse Laplace transfrom to each term and write the solution to the IVP using the Heavyside function.
5. Write the solution as a piecewise function (i.e., not using the Heavyside function).
