# MATH 3110-Fall 2015 

Homework 3
Due: Thursday September 17

## ALWAYS MOTIVATE THE ANSWERS!

## Questions. Chapter 3 of Strang

(total of 6 marks)

1. (a) Describe the column space of $A=\left(\begin{array}{ccc}1 & 1 & 0 \\ 0 & -1 & 1 \\ 1 & 0 & 1\end{array}\right)$. Which subspace is it?
(b) Construct a $3 \times 3$ matrix whose column space contains vectors $\left(\begin{array}{l}1 \\ 2 \\ 3\end{array}\right),\left(\begin{array}{l}1 \\ 0 \\ 1\end{array}\right)$ and not $\left(\begin{array}{l}1 \\ 1 \\ 1\end{array}\right)$
(c) Construct a $3 \times 3$ matrix whose column space is a line.
(2 marks)
(2 marks)

## Questions. Chapter 3 of Strang

1. Prove the following statements about the vector space $\mathbb{M}$ of $3 \times 3$ matrices
(a) The set of upper triangular matrices is a subspace of $\mathbb{M}$.
(b) The union of the following sets

- upper triangular matrices of $\mathbb{M}$, and
- lower triangular matrices of $\mathbb{M}$
is not a vector space of $\mathbb{M}$. (Find an example.)
(c) The set of symmetric matrices is a subspace of $\mathcal{M}$

2. Compute the row reduced echelon form of the following matrices

$$
A=\left(\begin{array}{lllll}
1 & 2 & 2 & 3 & 9 \\
3 & 6 & 1 & 4 & 7 \\
0 & 0 & 1 & 1 & 4
\end{array}\right) \text { and } B=\left(\begin{array}{lll}
1 & 1 & 1 \\
1 & 1 & 1 \\
2 & 3 & 3 \\
4 & 1 & 1 \\
1 & 2 & 3
\end{array}\right)
$$

3. Find the special solutions of the nullspace of the following matrices

$$
A=\left(\begin{array}{llll}
1 & 0 & 3 & 5 \\
0 & 1 & 1 & 2 \\
0 & 0 & 0 & 0
\end{array}\right) \quad \text { and } \quad B=\left(\begin{array}{cccc}
0 & 1 & 2 & 0 \\
0 & 0 & 0 & 1 \\
0 & 0 & 0 & 0
\end{array}\right)
$$

4. Construct a matrix $A$ such that $N(A)$ contains all multiples of $\left(\begin{array}{l}0 \\ 1 \\ 2 \\ 1\end{array}\right)$.
