MATH 3110 - Fall 2016

Homework 6

Due: October 6, 2016

QUESTION 1. Chapter 3 of Strang

(total of 20 marks)

1. (a) Give a basis of the four fundamental subspaces of the matrix

$$A = \left(\begin{array}{ccccc} 3 & 6 & 2 & -1 & -1 \\ 1 & 2 & 2 & 2 & 11 \\ 0 & 0 & 2 & -3 & 4 \\ 1 & 2 & 0 & 5 & 7 \end{array}\right).$$

(b) Determine the subspace the following vectors belong to:

(6 marks)

(8 marks)

$$v_1 = \begin{pmatrix} 0 \\ 0 \\ 0 \\ 0 \\ 0 \end{pmatrix}, v_2 = \begin{pmatrix} 0 \\ 0 \\ 0 \\ 0 \\ 0 \end{pmatrix}, v_3 = \begin{pmatrix} 2 \\ 3 \\ -3 \\ 6 \end{pmatrix}, v_4 = \begin{pmatrix} -1 \\ 2 \\ -5 \\ -2 \\ 1 \end{pmatrix}, v_5 = \begin{pmatrix} 0 \\ 4 \\ -4 \\ -4 \end{pmatrix} \text{ and } v_6 = \begin{pmatrix} 0 \\ 0 \\ 2 \\ 2 \\ 14 \end{pmatrix}.$$

2. Determine if the following subsets are subspaces and if they are find one of their basis.

(6 marks)

(a)
$$V = \langle \begin{pmatrix} 1\\2\\0\\3 \end{pmatrix}, \begin{pmatrix} 0\\1\\2\\4 \end{pmatrix}, \begin{pmatrix} 1\\1\\-2\\-1 \end{pmatrix} \rangle$$

(b)
$$V = \left\{ \begin{pmatrix} x_1 \\ x_2 \\ x_3 \end{pmatrix} \mid x_2 = x_1 - x_3 + 1 \right\}$$

(c)
$$V = \left\{ \begin{pmatrix} x_1 \\ x_2 \\ x_3 \\ x_4 \end{pmatrix} \mid x_1 = 0, \ x_2 = x_3 - x_4 \right\}$$