MATH 3110 - Fall 2017 **Homework 8**

Due: Thursday October 26

QUESTION 1. Chapter 4.2 of Strang

1. Determine which of the following matrices is a projection matrix (motivate your answer). For the projection matrices, find the subspace they project onto and its orthogonal complement (give a basis for each of them).

(a)
$$A_1 = \begin{pmatrix} \frac{1}{2} & 0 & 0 & \frac{1}{2} \\ 0 & \frac{1}{2} & \frac{1}{2} & 0 \\ 0 & \frac{1}{2} & \frac{1}{2} & 0 \\ \frac{1}{2} & 0 & 0 & \frac{1}{2} \end{pmatrix}$$
 (b) $A_2 = \begin{pmatrix} \frac{1}{2} & 0 & 0 & \frac{1}{2} \\ 0 & \frac{1}{2} & \frac{1}{2} & 0 \\ 0 & \frac{1}{2} & -\frac{1}{2} & 0 \\ -\frac{1}{2} & 0 & 0 & \frac{1}{2} \end{pmatrix}$ (c) $A_2 = \begin{pmatrix} \frac{1}{2} & 0 & 0 & -\frac{1}{2} \\ 0 & \frac{1}{2} & -\frac{1}{2} & 0 \\ 0 & -\frac{1}{2} & \frac{1}{2} & 0 \\ -\frac{1}{2} & 0 & 0 & \frac{1}{2} \end{pmatrix}$

QUESTION 2. Chapter 4.3 of Strang

- 1. Consider the four data points $(x_i, y_i) = (0, 0), (1, 8), (3, 8)$ and (4, 20).
 - (a) Find the best fitting line y = A + Bx between the points.
 - (b) Find the best fitting parabola $y = Cx^2 + Dx + E$ between the points

QUESTION 3. Chapter 4.4 of Strang

1. Compute using Gram-Schmidt the orthonormal basis of \mathbb{R}^4 related to the following basis vectors

$$v_1 := \begin{pmatrix} 2\\0\\0\\-2 \end{pmatrix}, \ v_2 := \begin{pmatrix} 2\\0\\0\\0 \end{pmatrix}, \ v_3 := \begin{pmatrix} 1\\1\\1\\1 \end{pmatrix} \text{ and } v_4 := \begin{pmatrix} 0\\2\\0\\-2 \end{pmatrix}.$$

(total of 6 marks)

(total of 6 marks)

(total of 8 marks)