# MATH 3110 - Fall 2018 <br> Homework 6 

Due: October 11, 2018

1. (a) Give a basis for each of the four fundamental subspaces of the matrix

$$
A=\left(\begin{array}{ccccc}
3 & 6 & 2 & -1 & -1 \\
1 & 2 & 2 & 2 & 11 \\
0 & 0 & 2 & -3 & 4 \\
1 & 2 & 0 & 5 & 7
\end{array}\right)
$$

(b) Determine which of the above subspaces the following vectors belong to:
(8 marks)

$$
v_{1}=\left(\begin{array}{l}
0 \\
0 \\
0 \\
0
\end{array}\right), v_{2}=\left(\begin{array}{l}
0 \\
0 \\
0 \\
0 \\
0
\end{array}\right), v_{3}=\left(\begin{array}{c}
2 \\
3 \\
-3 \\
6
\end{array}\right), v_{4}=\left(\begin{array}{c}
-1 \\
2 \\
-5 \\
-2 \\
1
\end{array}\right), v_{5}=\left(\begin{array}{c}
0 \\
4 \\
-4 \\
-4
\end{array}\right) \text { and } v_{6}=\left(\begin{array}{c}
0 \\
0 \\
2 \\
2 \\
14
\end{array}\right)
$$

2. Determine if the following subsets are subspaces and if they are find their basis.
(a) $V=\left\langle\left(\begin{array}{l}1 \\ 2 \\ 0 \\ 3\end{array}\right),\left(\begin{array}{c}-1 \\ -2 \\ 0 \\ -3\end{array}\right),\left(\begin{array}{l}0 \\ 1 \\ 2 \\ 4\end{array}\right),\left(\begin{array}{c}1 \\ 1 \\ -2 \\ -1\end{array}\right)\right\rangle$
(b) $V=\left\{\left.\left(\begin{array}{l}x_{1} \\ x_{2} \\ x_{3}\end{array}\right) \right\rvert\, x_{3}+1=x_{1}-x_{2}\right\}$
(c) $V=\left\{\left.\left(\begin{array}{l}x_{1} \\ x_{2} \\ x_{3} \\ x_{4}\end{array}\right) \right\rvert\, x_{1}=-x_{2}, x_{2}=x_{3}-x_{4}\right\}$
