MAT 129 Lab #3 February 26, 2007

- (1) Prove or disprove that $(x \lor y) \Rightarrow z$ is logically equivalent to $(x \Rightarrow z) \lor (y \Rightarrow z)$.
- (2) How many five-digit numbers are there that do not have two consecutive digits the same? *Note:* The first digit may not be zero.
- (3) A bookshelf contains 20 books. In how many different orders can these books be arranged on the shelf?
- (4) A class contains ten boys and ten girls. In how many different ways can they stand in line if they must alternate in gender (-ie. no two boys and no two girls are allowed to stand next to each other)?
- (5) Prove that $(x \wedge y) \lor (x \wedge \neg y)$ is logically equivalent to x.