# MTHSC 206 Section 12.1 – Three dimensional coordinate systems

Kevin James

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## Goal

We wish to generalize the familiar xy-plane to three dimensions in order to model the three dimensional space we live in. In order to do this we need to introduce some new ideas.

- We use the traditional x- and y-axes and add a third z-axis which is perpendicular to the xy-plane.
- The positive direction along the *z*-axis will be determined by the so called *right-hand rule*.
- To each point P in space we associate a 3-tuple (a, b, c).
- To arrive at the point *P*, we travel *a* units along the *x*-axis, *b* units in the direction parallel to the *y*-axis and *c* units in the direction parallel to the *z*-axis.

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### Note

There three planes determined by any two of the 3 axes are called the *xy*-plane, the *xz*-plane and the *yz*-plane.

#### EXERCISE

What solution spaces are determined by the following?

- *z* = 1.
- x = y.
- x = y = z.
- x = 2, y = 1, z = 3.

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## **DEFINITION** (DISTANCE FORMULA)

The distance  $|P_1P_2|$  between two points  $P_1(x_1, y_1, z_1)$  and  $P_2(x_2, y_2, z_2)$  is given by

$$|P_1P_2| = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2 + (z_2 - z_1)^2}$$

#### Note

This formula follows from the Pythagorean theorem.

#### EXERCISE

Find the distance between (2, 1, 3) and (1, -1, 5).

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## EXERCISE

Give an equation whose solution set is the points on the surface of the sphere centered at the point (h, k, l) and whose radius is r.

#### EXERCISE

What region of  $\mathbb{R}^3$  is determined by the following inequalities.

$$1 \le x^2 + y^2 + z^2 \le 4, \quad z \le 0$$

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