

**MATH 3190**  
**Sequences and Series Homework**  
**Due 23 February 2015**

**Name:** \_\_\_\_\_

You may not use your notes. Please show all of your work. An answer without justification will receive little credit.

- (1) Compute  $\lim_{n \rightarrow \infty} \frac{n^2+3n+1}{4n^2}$ . Prove your answer.
- (2) Compute  $\lim_{n \rightarrow \infty} \frac{n^2+3n+1}{3n^3}$ . Prove your answer.
- (3) Compute  $\lim_{n \rightarrow \infty} \frac{n+1}{3n+2}$ . Prove your answer.
- (4) Compute  $\sum_{n \geq 0} \left(\frac{2}{3}\right)^n$ .
- (5) Compute  $\sum_{n \geq 0} \left(\frac{1}{9}\right)^n$ .
- (6) Compute  $\sum_{n \geq 2} \left(\frac{1}{9}\right)^n$ .
- (7) Show that  $\sum_{n \geq 0} (-1)^n$  does not exist. Note that this will involve negating the statement that the limit does exist which involves 3 quantifiers. Be careful.