Subgroups generated by subsets of a Group

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Definition

Suppose that G is a group and that $A \subseteq G$. Then we define the the subgroup generated by A to be $< A >= \cap_{A \subseteq H \leq G} H$

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