

MTHSC 208 (Differential Equations)
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HW 8
Due Wednesday September 23rd, 2009

For full credit, be sure to *show your work* on all of these problems!

- (1) If $y_f(t)$ is a solution of

$$y'' + py' + qy = f(t)$$

and $y_g(t)$ is a solution of

$$y'' + py' + qy = g(t),$$

show that $z(t) = \alpha y_f(t) + \beta y_g(t)$ is a solution of

$$y'' + py' + qy = \alpha f(t) + \beta g(t),$$

where α and β are any real numbers.

- (2) Find the general solution to the following 2nd order linear homogeneous ODEs.
- (a) $y'' + 2y + 2y = 2 + \cos 2t$
 - (b) $y'' + 25y = 2 + 3t + 4 \cos 2t$
 - (b) $y'' - y = t - e^{-t}$.
- (3) (a) Find the general solution of $y'' + 3y' + 2y = te^{-4t}$. (Look for a particular solution of the form $y_p = (at + b)e^{-4t}$.)
- (b) Use a similar approach as above to find a solution to the differential equation $y'' + 3y' + 2y = t^2e^{-2t}$.
- (4) Find the general solution of $y'' + 2y' + 2y = e^{-2t} \sin t$. (Look for a particular solution of the form $y_p = e^{-2t}(a \cos t + b \sin t)$.)
- (5) For the following exercises, rewrite the give function in the form

$$y = A \cos(\omega t - \phi) = A \cos \left(\omega \left(t - \frac{\phi}{\omega} \right) \right),$$

and then plot the graph of this function.

- (a) $y = \cos 2t + \sin 2t$
- (b) $y = \cos t - \sin t$
- (c) $y = \cos 4t + \sqrt{3} \sin 4t$
- (d) $y = -\sqrt{3} \cos 2t + \sin 2t$.