

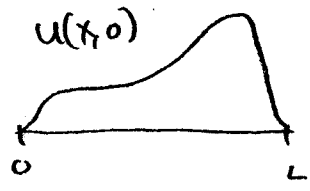
Week 12 summary:

• Parseval's identity: $\langle f(x), f(x) \rangle = \frac{1}{\pi} \int_{-\pi}^{\pi} (f(x))^2 dx = \frac{1}{2} a_0^2 + \sum_{n=1}^{\infty} a_n^2 + b_n^2$

Can be used for computing sums! e.g., $\sum_{n=1}^{\infty} \frac{1}{n^2} = \frac{\pi^2}{6}$

• Partial differential equations (PDE's): Equations involving a multivariate function and its partial derivatives.

* Heat equation: $u_t = c^2 u_{xx}$, $u(x,t)$ = temp at pos. x , time t .



* Boundary conditions, e.g., $u(0,t) = u(L,t) = 0$

* Initial condition: e.g., $u(x,0) = h(x)$
(initial temp. of bar).