MthS 4560/6560: Topology

Fall 2013

Long Hall, Room 123, TTh 12:30-1:45

- Instructor Dr. Matt Macauley (macaule@clemson.edu) **OFFICE:** Martin Hall O-325 PHONE: (864) 656–1838 (no voicemail!) OFFICE HOURS: (subject to change!) TTh 11:00-12:00, or by appointment WEBSITE: http://www.math.clemson.edu/~macaule/classes/f13_mthsc412/
- Textbook Introduction to Topology (Third Edition), by Bert Mendelson. Available new for \$8.45 on Amazon.
- Prerequisites MthS 1190/3190 (Intro to proofs), or any higher-level proof-based course (e.g., MthS 4120 or 4530).
- Overview This course is intended to be an introduction to the study of topology, with the focus on point-set topology. Geometry is the study of objects preserved by rigid motions, whereas topology is the study of properties of spaces and objects preserved by continuous deformations. Topology can be thought of "real analysis without the metric," in that one defines the open and closed sets of a space, and then studies traditional properties of the real numbers such as neighborhoods, continuous functions, compact sets, connected sets, and more. Topology plays a fundamental role in a wide range of areas of pure and applied mathematics and physics, from algebraic geometry, to data analysis, to general relativity to string theory, just to name a few. It is a must for students who plan to pursue mathematics in graduate school and is strongly recommended for physics majors.
- Topics Basic review of the theory of sets. Introduction to metric spaces, and topics such as continuity, open balls, limits, and open and closed sets. Introduction to topological spaces, and topics such as neighborhoods, closure, interior, boundary, functions, continuity, homeomorphism, subspaces, and products. Compactness in topological spaces, the real line, and in metric spaces. Connectedness and path-connectedness of topological spaces, and homotopic paths and the fundamental group.

Learning By taking this class, students will:

Outcomes

- Demonstrate a solid understand of point-set topology and basic homotopy theory at the undergraduate level.
- Abstract the notion and key properties of a metric space to a general topological space.
- Explain to a friend or family member who knows nothing about mathematics • what topology is, why we should study it, and why it might be fun to do so!
- Learn to understand, read, and write rigorous mathematical proofs on topology. ٠
- Further develop and improve good mathematical writing skills. Important aspects of this are *accuracy*, *clarity*, and *conciseness*.

| Policies | • Homework assignments will accumulate from lecture to lecture and will be due roughly once a week. I will post the problems on my website. Late homework will <i>not</i> be accepted. | |
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| | • Attendance is not mandatory, but highly recommended. | |
| | • If you get an A or B course, provided you passing grade on the | B on the final exam, then you get at least that grade in the have (i) attended class <i>very</i> regularly, and (ii) maintain a b homework. |
| | • All drop/add procedures are your responsibility. | |
| | Absent Professor Policy: If the instructor has not arrived within 15 minutes of the scheduled class time, you may assume that class has been canceled. All use of cell phones, laptops, and PDAs is prohibited during lecture. Calculators, cell phones, laptops, and PDAs will not allowed during exams. Cell phone policy: http://www.youtube.com/watch?v=FYwpxU_G4Z0 | |
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| • No whining. | | |
| Grading | The final grade will be calculated as follows: | |
| | Homework: | 25% |
| | MIDTERM 1: | 25% |
| | MIDTERM 2: | 25% |
| | F'INAL EXAM: | 50% |
| | I will drop either your lowest midterm, or half the weight of your final exam. | |
| Homework | Homework assignments will accumulate from lecture to lecture and will be due several times a week. I will post the assignments on my website, as I like to make all materials freely available to everybody (Warning: Websites such as <i>Course Hero</i> are a SCAM!). Students may collaborate on their homework problems, but they <i>must</i> write up and submit their homeworks separately as well as document their collaborators. Late homeworks will not be accepted. You are encouraged to typeset your homework assignments (LATEXpreferred but not required), and you will get an extra night to complete it if you do (okay to hand-draw pictures, though – there will be many!). You should keep all the graded homeworks in case of missing grades due to missing name or typo errors. | |
| Key Dates | August 22 (Thu) August 27 (Tue) September 3 (Tue) | Class begins; late enrollment fee applies Last day to register or add a class Last day to drop a class or withdraw from the University without a W grade |
| | October 14–15 (M–Tu) October 29 (Tue) | Fall break Last day to drop a class or withdraw from the University |
| | N | without final grades |
| | November $2(-29 (W-F))$ | I nanksgiving break |
| | December 9 (Mon) | MthS $4560/6560$ Final Exam $(3.00-5.30$ pm) |
| | | (0.00 0.00pm) |

The official statement on Academic Integrity

As members of the Clemson University community, we have inherited Thomas Green Clemson's vision of this institution as a *high seminary of learning*. Fundamental to this vision is a mutual commitment to truthfulness, honor, and responsibility, without which we cannot earn the trust and respect of others. Furthermore, we recognize that academic dishonesty detracts from the value of a Clemson degree. Therefore, we shall not tolerate lying, cheating, or stealing in any form. When in the opinion of a faculty member, there is evidence that a student has committed an act of academic dishonesty, the faculty member shall make a formal written charge of academic dishonesty including a description of the misconduct, to the Dean of the Graduate School. At the same time, the faculty member may, but is not required to, inform each involved student privately of the nature of the alleged charge.