

## MthSc 208: Differential Equations (Summer II, 2010)

### In-class Worksheet 1a: Plotting slope fields

NAME:

Consider the ODE  $y' = 2y + t$ .

- (a) Draw the  $ty$ -plane (i.e.,  $t$  on the  $x$ -axis, and  $y(t)$  on the  $y$ -axis). Draw a dot at each integer lattice point at each  $(t, y)$ , where  $t, y = -1, 0, 1$ .

- (b) At each of these nine points, compute  $y'(t)$ . On the  $ty$ -plane, draw a “hash mark” at  $(t, y)$  with slope  $y'(t)$ .

- (c) Now, we will use a better method to sketch the slope field. Determine the set of points for which  $y' = 0$  (it will be a line – set  $y' = 0$  and solve for  $y$ .)
- (d) Repeat the previous step except for  $y' = c$ , for various values of  $c$ : 1, 2, 3,  $-1$ ,  $-\frac{1}{2}$ .
- (e) Sketch the lines you found above on the  $ty$ -plane. Along each line, sketch the hash-marks of the corresponding slope,  $y' = c$ .
- (f) In the slope field above, sketch the three particular solution curves that satisfy  $y(0) = 1$ ,  $y(0) = -\frac{3}{4}$ , and  $y(1) = -\frac{3}{4}$ , respectively.