MthSc 208: Differential Equations (Summer I, 2013) In-class Worksheet 5f: ODEs with Piecewise Forcing Terms

NAME:

Consider the initial value problem y'' + y = f(t), y(0) = 0, y'(0) = 1, where $f(t) = \begin{cases} 2t, & 0 \le t \le 1\\ 2, & t > 1 \end{cases}$

1. Sketch f(t), and write it using the Heavyside function.

2. Take the Laplace transform of the differential equation, and solve for Y(s).

3. Use partial fractions to decompose Y(s) into four terms. [Note: $\frac{1}{s^2(s^2+1)} = \frac{1}{s^2} - \frac{1}{s^2+1}$.]

4. Apply the inverse Laplace transfrom to each term and write the solution to the IVP using the Heavyside function.

5. Write the solution as a piecewise function (i.e., not using the Heavyside function).