# Math 2080: Differential Equations Worksheet 1.1: What is a differential equation? 

## NAME:

1. Consider an investment that grows at a constant interest rate of $5 \%$, compounded continuously. Suppose that initially, the investment is worth $\$ 1000$. If $P(t)$ is the value of the investment, write out an initial value problem (IVP) - a differential equation with an initial condition - that $P(t)$ satisfies and sketch the solutions.
2. Consider an investment that grows at a constant interest rate of $5 \%$, compounded continuously. Suppose that initially, the investment is growing at a rate of $\$ 100 / \mathrm{year}$. If $P(t)$ is the value of the investment, write out an IVP that $P(t)$ satisfies and sketch the solutions.
3. The mass $m(t)$ of a radioactive substance decays at a rate proportional to the amount remaining. Suppose there are 100 grams initially. Write out an IVP that $m(t)$ satisfies and sketch the solutions.
4. The temperature $T(t)$ of a cup of coffee cools at a rate proportional to the difference in its temperature with the ambient room temperature (say, $70^{\circ}$ ). Suppose that the coffee is initally $190^{\circ}$.
(a) Write out an initial value problem that $T(t)$ satisfies and sketch the solutions.
(b) Let $y(t)=T(t)-70$, which represents the number of degrees that the coffee is above or below the room temperature. Substituting $T=y+70$ back into your IVP from the previous part to get a much simplier IVP in terms of the function $y(t)$ and sketch the solutions.
