## Math 2080: Differential Equations

## Worksheet 4.5: Phase portraits with real eigenvalues

## NAME:

Suppose the eigenvalues and eigenvectors of a $2 \times 2$ matrix $\boldsymbol{A}$ are given. Write the general solution to the system $\boldsymbol{x}^{\prime}=\boldsymbol{A} \boldsymbol{x}$. Then, sketch the phase portrait (the graph $x_{2}$ vs. $x_{1}$ ). Make sure that your sketch is accurate enough that it is clear which way the solution curves "bend", if applicable. Also, you should clearly distinguish between e.g., a line of slope 2 and a line of slope $1 / 2$.

1. $\lambda_{1}=-2, \lambda_{2}=2, \mathbf{v}_{1}=\left[\begin{array}{l}1 \\ 2\end{array}\right], \mathbf{v}_{2}=\left[\begin{array}{c}-3 \\ 1\end{array}\right]$.
2. $\lambda_{1}=-2, \lambda_{2}=-3, \mathbf{v}_{1}=\left[\begin{array}{l}1 \\ 2\end{array}\right], \mathbf{v}_{2}=\left[\begin{array}{c}-3 \\ 1\end{array}\right]$.
3. $\lambda_{1}=-2, \lambda_{2}=-30, \mathbf{v}_{1}=\left[\begin{array}{l}1 \\ 2\end{array}\right], \mathbf{v}_{2}=\left[\begin{array}{c}-3 \\ 1\end{array}\right]$.
4. $\lambda_{1}=2, \lambda_{2}=3, \mathbf{v}_{1}=\left[\begin{array}{l}1 \\ 2\end{array}\right], \mathbf{v}_{2}=\left[\begin{array}{c}-3 \\ 1\end{array}\right]$.
5. $\lambda_{1}=0.2, \lambda_{2}=3, \mathbf{v}_{1}=\left[\begin{array}{l}1 \\ 2\end{array}\right], \mathbf{v}_{2}=\left[\begin{array}{c}-3 \\ 1\end{array}\right]$.
6. $\lambda_{1}=0, \lambda_{2}=3, \mathbf{v}_{1}=\left[\begin{array}{l}1 \\ 2\end{array}\right], \mathbf{v}_{2}=\left[\begin{array}{c}-3 \\ 1\end{array}\right]$.
