

**Problem 1.** Prove if  $a, b \in \mathbb{R}$  and  $ab$  is irrational, then at least one of  $a$  or  $b$  is irrational.

**Problem 2.** Let  $n \in \mathbb{Z}$ . Prove that if  $n^2$  is divisible by 3, then  $n$  is divisible by 3.

**Problem 3.** Prove that  $\sqrt{2} + \sqrt{3}$  is irrational. [Hint: Suppose it were. Try solving for  $\sqrt{3}$ .]

**Problem 4.** We proved the statement "*if  $n^2$  is even, then  $n$  is even*" using the contrapositive. Alternatively, write a proof of this by contradiction.