MATH 3110 - Fall 2014 Homework 10

Due: Thursday November 13

Questions. Chapter 6.1 and 6.2 of Strang

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(total of 20 marks)

(10 marks)

(5 marks)

1. Compute the eigenvalues and the eigenvectors of the following matrices if possible.

(a)
$$A = \begin{pmatrix} 5 & -2 \\ 4 & -1 \end{pmatrix}$$

(b) $B = \begin{pmatrix} -3 & -3 & 6 \\ 6 & 6 & -6 \\ 0 & 0 & 3 \end{pmatrix}$
(c) $C = \begin{pmatrix} 4 & 1 \\ -1 & 2 \end{pmatrix}$
(d) $D = \begin{pmatrix} \frac{1}{2} & -\frac{\sqrt{3}}{2} & 0 \\ \frac{\sqrt{3}}{2} & \frac{1}{2} & 0 \\ 0 & 0 & 1 \end{pmatrix}$
2. Diagonalize matrix $A = \begin{pmatrix} 0 & 0 & 1 \\ 0 & 1 & 0 \\ 1 & 0 & 0 \end{pmatrix}$ by finding the matrices S and Λ . (5 marks)

3. Diagonalize A and compute $S\Lambda^kS^{-1}$ to prove this formula for A^k

$$A = \begin{pmatrix} 2 & -1 \\ -1 & 2 \end{pmatrix} \text{ and } A^{k} = \frac{1}{2} \begin{pmatrix} 1+3^{k} & 1-3^{k} \\ 1-3^{k} & 1+3^{k} \end{pmatrix}$$