Online Supplement to "Minimum Spanning Trees in Networks with Varying Edge Weights"

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Figures

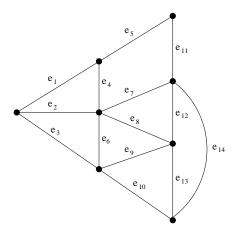


Figure 1: Network *Alex1*.

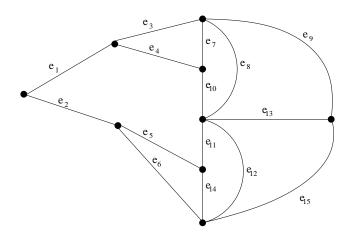


Figure 2: Network *Alex2*.

Tables

Edge	Weight	Probability
e_1	$\{70, 94\}$	$\{0.95, 0.05\}$
e_2	$\{25, 52\}$	$\{0.8, 0.2\}$
e_3	$\{42,61\}$	$\{0.7, 0.3\}$
e_4	$\{15, 43\}$	$\{0.8, 0.2\}$
e_5	$\{26, 50\}$	$\{0.85, 0.15\}$
e_6	$\{21, 68\}$	$\{0.9, 0.1\}$
e_7	$\{65, 75\}$	$\{0.6, 0.4\}$
e_8	$\{59, 78\}$	$\{0.7, 0.3\}$
e_9	$\{90, 96\}$	$\{0.95, 0.05\}$
e_{10}	$\{89, 96\}$	$\{0.85, 0.15\}$
e_{11}	$\{32,67\}$	$\{0.8, 0.2\}$
e_{12}	$\{16, 42\}$	$\{0.7, 0.3\}$
e_{13}	${3,15}$	$\{0.6, 0.4\}$
e_{14}	$\{17, 45\}$	$\{0.8, 0.2\}$

Table 1: Edge-weight random variables for Alex1-A.

Edge	Weight	Probability
e_1	$\{2, 8, 12\}$	$\{0.9, 0.08, 0.02\}$
e_2	$\{10, 24, 35\}$	$\{0.85, 0.12, 0.03\}$
e_3	$\{6, 18, 21\}$	$\{0.88, 0.1, 0.02\}$
e_4	$\{12, 22, 30\}$	$\{0.85, 0.11, 0.04\}$
e_5	$\{17, 35, 50\}$	$\{0.75, 0.2, 0.05\}$
e_6	${3,7,12}$	$\{0.84, 0.13, 0.03\}$
e_7	{10, 19, 24}	$\{0.8, 0.14, 0.06\}$
e_8	$\{4, 6, 10\}$	$\{0.75, 0.17.0.08\}$
e_9	$\{9, 13, 20\}$	$\{0.82, 0.15, 0.03\}$
e_{10}	$\{21, 33, 45\}$	$\{0.85, 0.09, 0.06\}$
e_{11}	{8, 14, 18}	$\{0.77, 0.13, 0.10\}$
e_{12}	{20, 30, 40}	$\{0.87, 0.09, 0.04\}$
e_{13}	{10, 17, 30}	$\{0.95, 0.03, 0.02\}$
e_{14}	$\{15, 28, 45\}$	$\{0.79, 0.15, 0.06\}$

Table 2: Edge-weight random variables for Alex1-B.

Edge	Weight	Probability
e_1	{70,94}	$\{0.95, 0.05\}$
e_2	$\{42,61\}$	$\{0.7, 0.3\}$
e_3	$\{26, 50\}$	$\{0.85, 0.15\}$
e_4	$\{58, 95\}$	$\{0.7, 0.3\}$
e_5	$\{90, 96\}$	$\{0.95, 0.05\}$
e_6	$\{89, 96\}$	$\{0.85, 0.15\}$
e_7	$\{60, 88\}$	$\{0.9, 0.1\}$
e_8	$\{32,67\}$	$\{0.8, 0.2\}$
e_9	$\{63, 99\}$	$\{0.75, 0.25\}$
e_{10}	$\{32,48\}$	$\{0.75, 0.25\}$
e_{11}	$\{16, 42\}$	$\{0.7, 0.3\}$
e_{12}	${3,15}$	$\{0.6, 0.4\}$
e_{13}	$\{56, 71\}$	$\{0.8, 0.2\}$
e_{14}	$\{17, 45\}$	$\{0.8, 0.2\}$
e_{15}	$\{50, 66\}$	$\{0.75, 0.25\}$

Table 3: Edge-weight random variables for Alex2-A.

Edge	Weight	Probability
e_1	$\{2, 8, 12\}$	{0.9, 0.08, 0.02}
e_2	$\{6, 18, 21\}$	$\{0.88, 0.1, 0.02\}$
e_3	$\{17, 35, 50\}$	$\{0.75, 0.2, 0.05\}$
e_4	${3,7,10}$	$\{0.68, 0.25, 0.07\}$
e_5	$\{9, 13, 20\}$	$\{0.82, 0.15, 0.03\}$
e_6	$\{21, 33, 45\}$	$\{0.85, 0.09, 0.06\}$
e_7	$\{18, 27, 36\}$	$\{0.94, 0.05, 0.01\}$
e_8	{8, 14, 18}	$\{0.77, 0.13, 0.10\}$
e_9	$\{15, 21, 25\}$	$\{0.76, 0.22, 0.02\}$
e_{10}	$\{25, 38, 50\}$	$\{0.8, 0.12, 0.08\}$
e_{11}	$\{20, 30, 40\}$	$\{0.87, 0.09, 0.04\}$
e_{12}	{10, 17, 30}	{0.95, 0.03, 0.02}
e_{13}	$\{4, 19, 15\}$	$\{0.75, 0.14, 0.11\}$
e_{14}	$\{15, 28, 45\}$	$\{0.79, 0.15, 0.06\}$
e_{15}	$\{8, 14, 25\}$	$\{0.85, 0.1, 0.05\}$

Table 4: Edge-weight random variables for Alex2-B.

Edge	Weight E1	Weight E2	Probability
e_1	$\{1,4,5,7\}$	$\{1, 5, 11, 22\}$	$\{0.25, 0.25, 0.25, 0.25\}$
e_2	$\{4, 6, 8, 10\}$	$\{4, 9, 12, 17\}$	$\{0.25, 0.25, 0.25, 0.25\}$
e_3	$\{3, 7, 9, 15\}$	$\{1, 7, 15, 19\}$	$\{0.25, 0.25, 0.25, 0.25\}$
e_4	{8, 9, 10, 11}	{6, 10, 14, 21}	$\{0.25, 0.25, 0.25, 0.25\}$
e_5	$\{5, 7, 10, 12\}$	$\{4,7,11,16\}$	$\{0.25, 0.25, 0.25, 0.25\}$
e_6	$\{2, 3, 6, 7\}$	$\{2, 3, 10, 15\}$	$\{0.25, 0.25, 0.25, 0.25\}$
e_7	$\{5,6,7,9\}$	{5, 10, 15, 29}	$\{0.25, 0.25, 0.25, 0.25\}$
e_8	{8, 12, 13, 15}	{6, 12, 18, 25}	$\{0.25, 0.25, 0.25, 0.25\}$
e_9	$\{1, 6, 9, 10\}$	$\{1,6,11,17\}$	$\{0.25, 0.25, 0.25, 0.25\}$
e_{10}	${3,5,7,9}$	${3,7,14,23}$	$\{0.25, 0.25, 0.25, 0.25\}$

Table 5: Edge-Weight Random Variables for $K_5\text{-}E1$ and $K_5\text{-}E2$

Edge	Weight E1	Weight E2	Probability
e_1	$\{1, 4, 5\}$	$\{1, 5, 11\}$	$\{0.333, 0.333, 0.333\}$
e_2	$\{4, 6, 8\}$	$\{4, 9, 12\}$	$\{0.333, 0.333, 0.333\}$
e_3	${3,7,9}$	$\{1, 7, 15\}$	$\{0.333, 0.333, 0.333\}$
e_4	$\{8, 9, 10\}$	$\{6, 10, 14\}$	$\{0.333, 0.333, 0.333\}$
e_5	$\{5, 7, 10\}$	$\{4, 7, 11\}$	$\{0.333, 0.333, 0.333\}$
e_6	$\{2, 3, 6\}$	$\{2, 3, 10\}$	$\{0.333, 0.333, 0.333\}$
e_7	$\{5, 6, 7\}$	$\{5, 10, 15\}$	$\{0.333, 0.333, 0.333\}$
e_8	$\{8, 12, 13\}$	$\{6, 12, 18\}$	$\{0.333, 0.333, 0.333\}$
e_9	$\{1, 6, 9\}$	$\{1, 6, 11\}$	$\{0.333, 0.333, 0.333\}$
e_{10}	${3,5,7}$	$\{3, 7, 14\}$	$\{0.333, 0.333, 0.333\}$
e_{11}	$\{4, 5, 8\}$	$\{4, 5, 13\}$	$\{0.333, 0.333, 0.333\}$
e_{12}	$\{9, 11, 12\}$	$\{2, 8, 12\}$	$\{0.333, 0.333, 0.333\}$
e_{13}	${3,4,6}$	${3,8,12}$	$\{0.333, 0.333, 0.333\}$
e_{14}	$\{5, 7, 9\}$	$\{5, 9, 12\}$	$\{0.333, 0.333, 0.333\}$
e_{15}	$\{1, 4, 8\}$	$\{1, 6, 11\}$	$\{0.333, 0.333, 0.333\}$

Table 6: Edge-Weight Random Variables for $K_6\text{-}E1$ and $K_6\text{-}E2$